

# SOLUZIONE MATEMATICA FINANZIARIA

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Ex1  $i_s = [(1+i_{Te})^2 - 1] = 10.25\%$

$$j(3) = 3[(1+i)^{\frac{1}{3}} - 1] = 0.0297 = 2.97\%$$

$$\delta = \log(1+i) = \log(1+i_{\frac{1}{2}})^2 = 2 \log(1+i_{\frac{1}{2}}) = 7.84\%$$

Ex2

$$6 R_m \ddot{s}_{\overline{60}|i_s}^{(6)} = 3 \bar{R}_m \cdot \ddot{s}_{\overline{80}|i_{Te}}^{(3)}$$

da cui  $R_m = ?$   $\bar{R}_m = 1200$ ;  $i_s = 9\%$ ;  $i_{Te} = 4\%$

$$R_m = \frac{3 \bar{R}_m \cdot \ddot{s}_{\overline{80}|i_{Te}}^{(3)}}{6 \ddot{s}_{\overline{60}|i_s}^{(6)}} = \frac{1200 \cdot \frac{i_{Te}}{j_{Te}(3)} \cdot \ddot{s}_{\overline{80}|i_{Te}}}{2 (1+i_s) \cdot \frac{i_s}{j_s(6)} \cdot \ddot{s}_{\overline{60}|i_s}}$$

$$= \frac{600 [1 - (1+i_{Te})^{-80}] \cdot j_s(6)}{(1+i_s) \cdot j_{Te}(3) \cdot [(1+i_s)^{60} - 1]} \approx 66,11 \text{ €}$$

Ex3

$$6 R_m \cdot \ddot{s}_{\overline{40}|i_s}^{(6)} = 120.000$$

$R_m = ?$   $i_s = 4\%$   
 $n = 20$

$$\Rightarrow R_m = \frac{120.000}{6 \cdot \frac{i_s}{j_s(6)} \cdot \frac{[(1+i_s)^{40} - 1]}{i_s}} = \frac{20.000 \cdot j_s(6)}{(1+i_s)^{40} - 1} \approx 207,1 \text{ €}$$

$$j_s(6) = 3.93\% \approx$$

[Ex 4]  $(\mathcal{C}, 0) \quad n=10$  diff:  $t=2$  anni, metodo Tabular

$$\bar{\mathcal{C}} = \mathcal{C}(1+i)^2 \quad \text{a } t=2 \quad \mathcal{C}_* = \frac{\bar{\mathcal{C}}}{10}$$

$$t=3 \quad I_1 = \bar{\mathcal{C}} \cdot i; \mathcal{C}_*; R_1 = \mathcal{C}_* + I_1; \mathcal{C}^{(1)} = \bar{\mathcal{C}} - \mathcal{C}_*$$

$$t=4 \quad I_2 = \mathcal{C}^{(1)} \cdot i; \mathcal{C}_*; R_2 = \mathcal{C}_* + I_2; \mathcal{C}^{(2)} = \bar{\mathcal{C}} - \mathcal{C}_* - \mathcal{C}_*$$

$$\vdots$$

$$t=12 \quad I_{10} = \mathcal{C}^{(9)} \cdot i; \mathcal{C}_*; R_{10} = \mathcal{C}_* + I_{10}; \mathcal{C}^{(10)} = \mathcal{C}^{(9)} - \mathcal{C}_* = 0$$

$$t=4 \quad \mathcal{C}_* = 0 \quad 2^{\text{o}} \text{ rete capite} \Rightarrow \tilde{\mathcal{C}}^{(2)} = \mathcal{C}^{(1)}$$

$$R = \frac{\tilde{\mathcal{C}}^{(2)}}{0,07i}$$

$$t=5 \quad 3^{\text{o}} \text{ rete: } \tilde{I}_3 = \tilde{\mathcal{C}}^{(2)} \cdot i; R; \tilde{\mathcal{C}}_3 = R - \tilde{I}_3; \tilde{\mathcal{C}} = \tilde{\mathcal{C}} - \tilde{\mathcal{C}}_3$$

$$\vdots$$

$$t=12 \quad 10^{\text{o}} \text{ rete: } \tilde{I}_{10} = \tilde{\mathcal{C}}^{(9)} \cdot i; R; \tilde{\mathcal{C}}_{10} = R - \tilde{I}_{10}; \tilde{\mathcal{C}} = \tilde{\mathcal{C}} - \tilde{\mathcal{C}}_{10} = 0$$

$$t=9 \quad 7^{\text{o}} \text{ rete: } \tilde{\mathcal{C}}_7 = 0 \Rightarrow \tilde{\mathcal{C}}^{(7)} = \tilde{\mathcal{C}}^{(6)}$$

$$t=10 \quad 8^{\text{o}} \text{ rete: } \tilde{I}^{(8)} = \tilde{\mathcal{C}}^{(7)} \cdot i; \quad \tilde{\mathcal{C}}^{(8)} = \tilde{\mathcal{C}}^{(7)} = \tilde{\mathcal{C}}^{(6)}$$

$$t=11 \quad 9^{\text{o}} \text{ rete: } \tilde{I}^{(9)} = \tilde{I}^{(8)} \quad \tilde{\mathcal{C}}^{(9)} = \tilde{\mathcal{C}}^{(8)}$$

$$t=12 \quad 10^{\text{o}} \text{ rete: } \tilde{I}^{(10)} = \tilde{I}^{(9)}; \tilde{\mathcal{C}}_{10} = \tilde{\mathcal{C}}^{(9)} = \tilde{\mathcal{C}}^{(6)}$$

$$\tilde{R}_{10} = \tilde{\mathcal{C}}_{10} + \tilde{I}^{(10)}; \quad \tilde{\mathcal{C}}^{(10)} = 0$$

mutuoluto

CASH-FLOW:

$$\left\{ (-C, 0) (R_1, 3) (I_2, 4) (R, 5) (R, 6) \text{ ~~(R, 7)~~ } (R, 8) (\tilde{I}_7, 9) (\tilde{I}_8, 10) (\tilde{I}_9, 11) (\tilde{R}_{10}, 12) \right\}$$

$$A^{(3)}(i_1) = I_1 (1+i_1)^{-1} + R \left[ (1+i_1)^{-2} + (1+i_1)^{-3} + (1+i_1)^{-4} + (1+i_1)^{-5} \right] + \\ + \tilde{I}_7 (1+i_1)^{-6} + \tilde{I}_8 (1+i_1)^{-7} + \tilde{I}_9 (1+i_1)^{-8} + \tilde{R}_{10} (1+i_1)^{-9}$$

NUOVA PROPRIETÀ:

$$K^{(3)}(i_1) = \tilde{C}_3 (1+i_1)^{-2} + \tilde{C}_4 (1+i_1)^{-3} + \tilde{C}_5 (1+i_1)^{-4} + \tilde{C}_6 (1+i_1)^{-5} + \\ + \tilde{C}_{10} (1+i_1)^{-9}$$

USUFRUTTO:

$$U^{(3)}(i_1) = I_1 (1+i_1)^{-1} + \tilde{I}_3 (1+i_1)^{-2} + \tilde{I}_4 (1+i_1)^{-3} + \tilde{I}_5 (1+i_1)^{-4} + \tilde{I}_6 (1+i_1)^{-5} + \\ + \tilde{I}_7 (1+i_1)^{-6} + \tilde{I}_8 (1+i_1)^{-7} + \tilde{I}_9 (1+i_1)^{-8} + \tilde{I}_{10} (1+i_1)^{-9}$$

VALUTAZIONE RETROSPETTIVA:

$$Z^{(3)}(i_1) = -C (1+i_1)^{13} + R_1 (1+i_1)^{10} + I_2 (1+i_1)^9 + R \left[ (1+i_1)^8 + (1+i_1)^7 + \right. \\ \left. + (1+i_1)^6 + (1+i_1)^5 \right] + \tilde{I}_7 (1+i_1)^4 + \tilde{I}_8 (1+i_1)^3 + \tilde{I}_9 (1+i_1)^2 + \\ + \tilde{R}_{10} (1+i_1)$$